

Imaging challenges in optical tomography

Dutch Inverse Problems, November 26st 2021

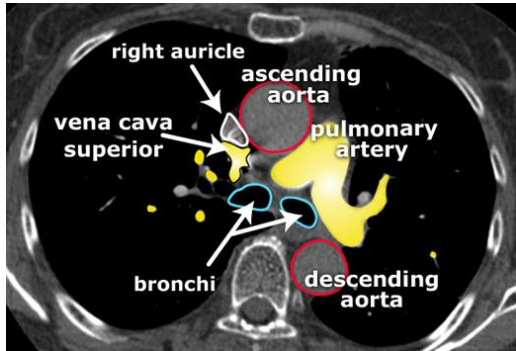
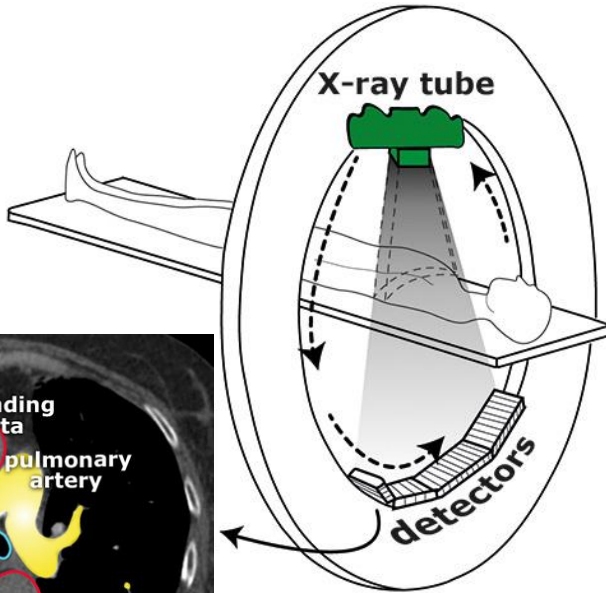
Jeroen Kalkman

Department of Imaging Physics, Delft University of Technology

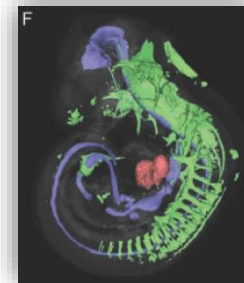
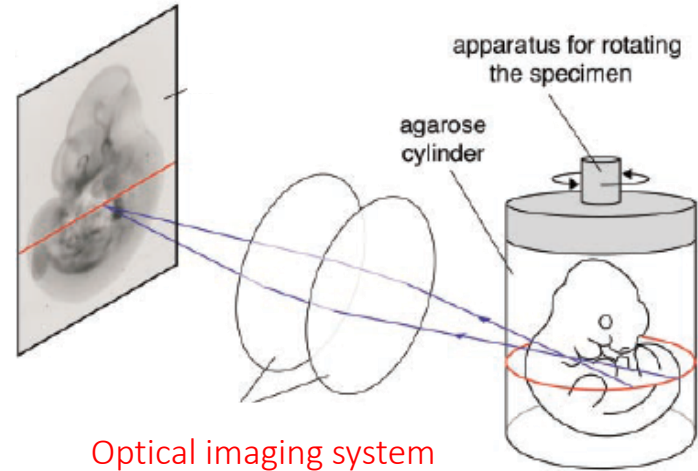


Optical versus X-ray tomography

X-ray tomography



Optical tomography



Challenges in optical tomography

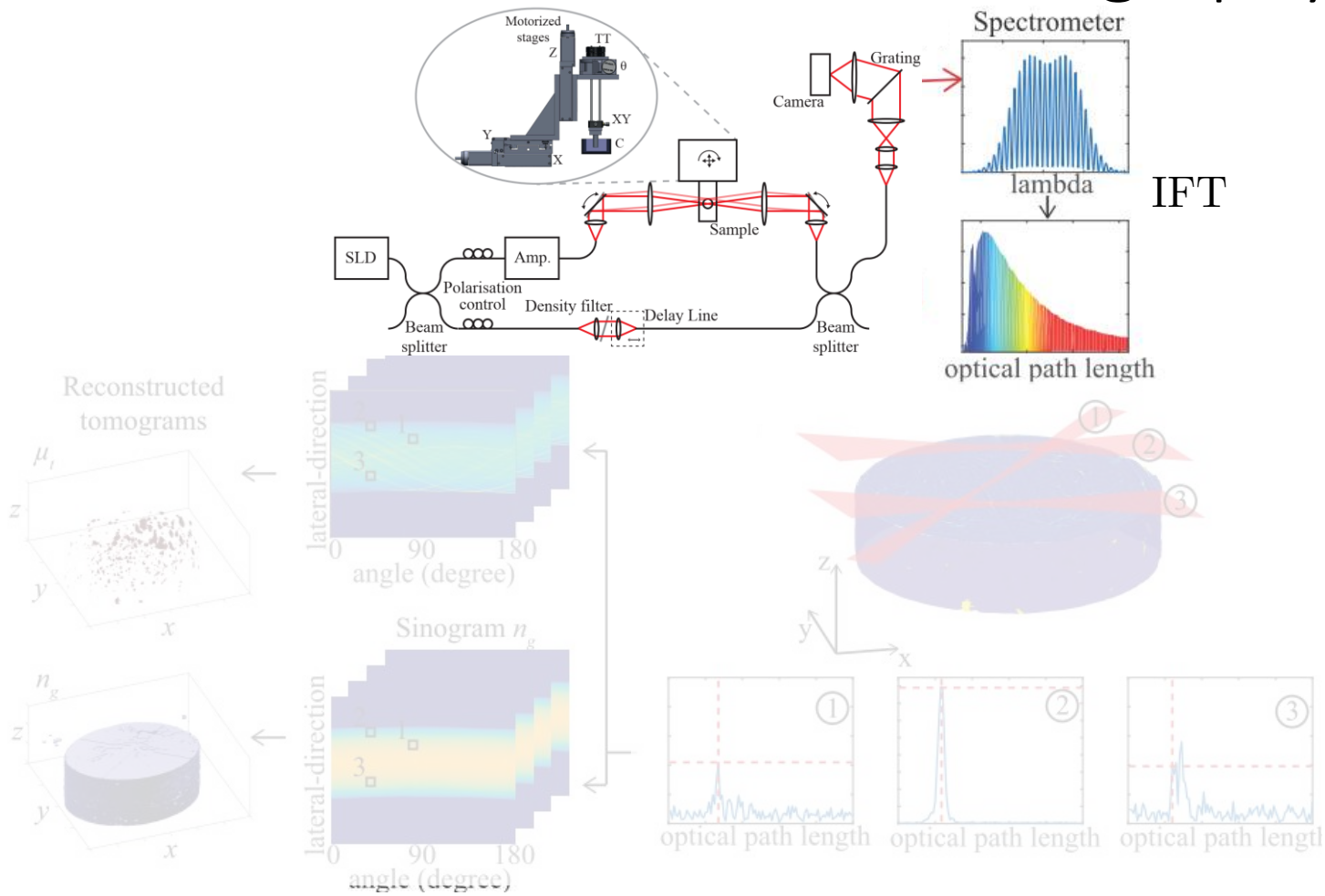


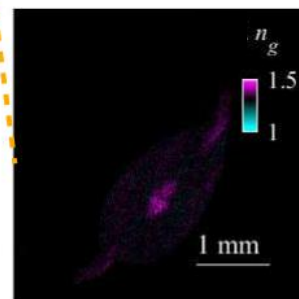
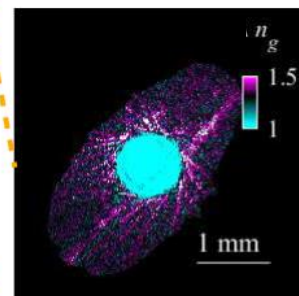
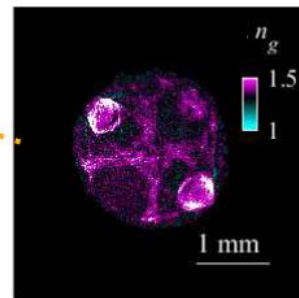
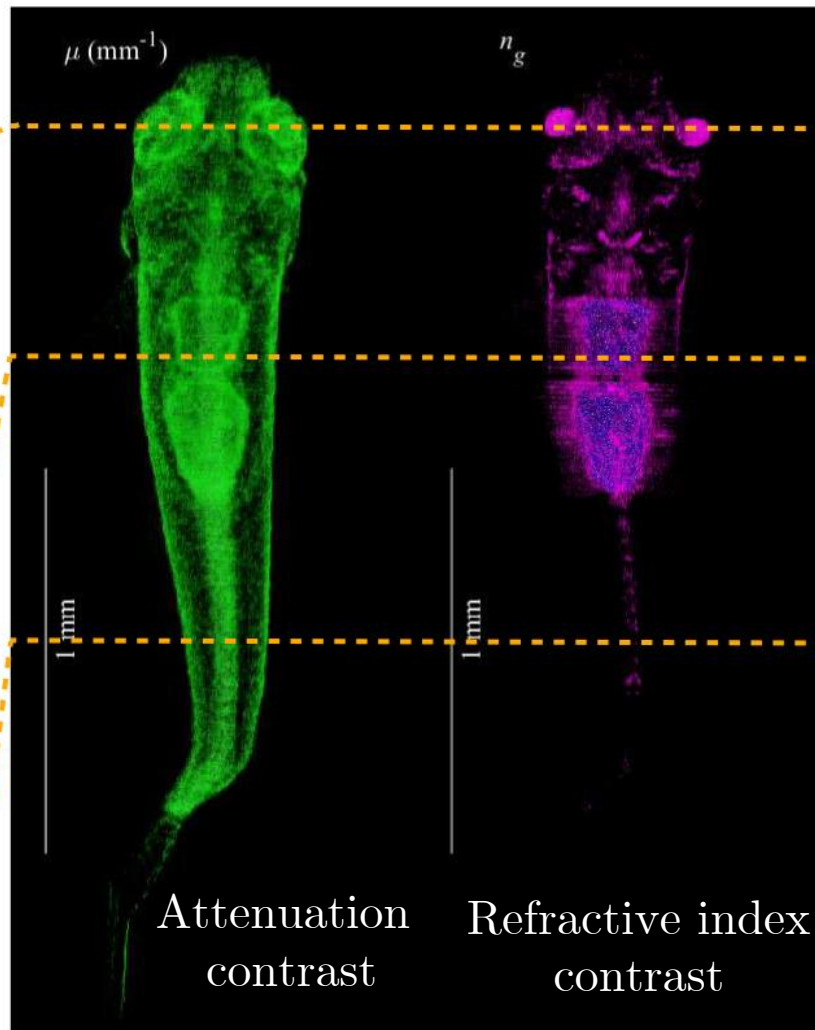
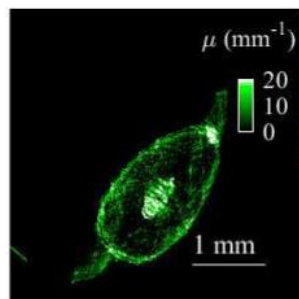
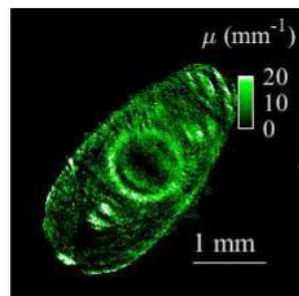
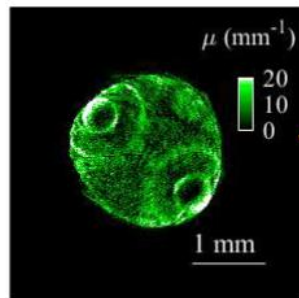
Scattering



Diffraction

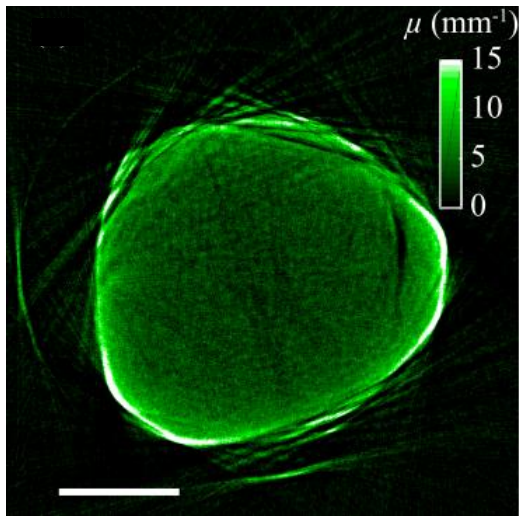
Optical coherence tomography



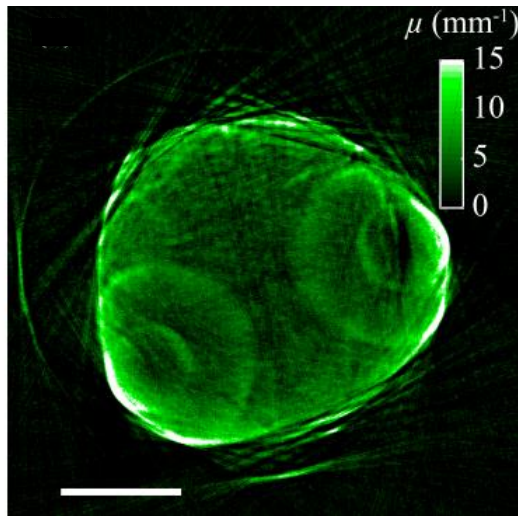


OCPT imaging depth analysis

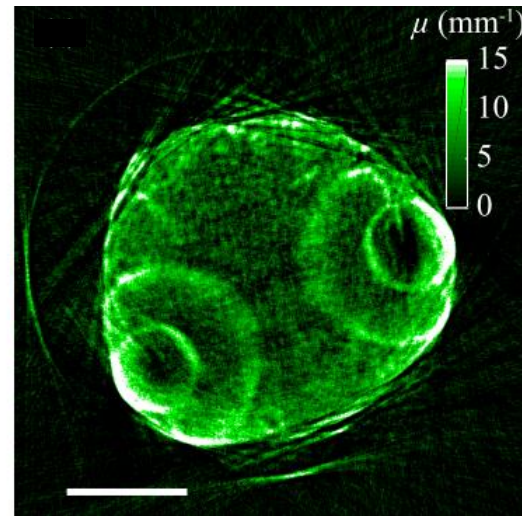
Confocal



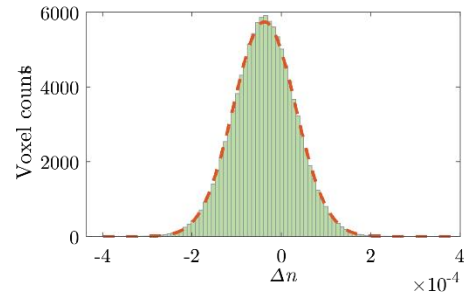
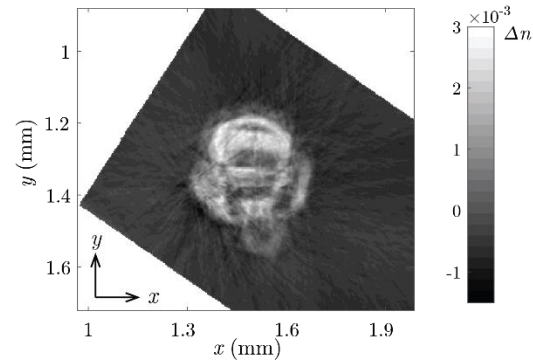
Confocal & coherence



Full OCPT imaging



Optical tomography: scattering



$$\Delta n = 8 \cdot 10^{-5}$$



H. Hama et al., Nature Neuroscience 14, 1481 (2011)

Challenges in optical tomography



Scattering



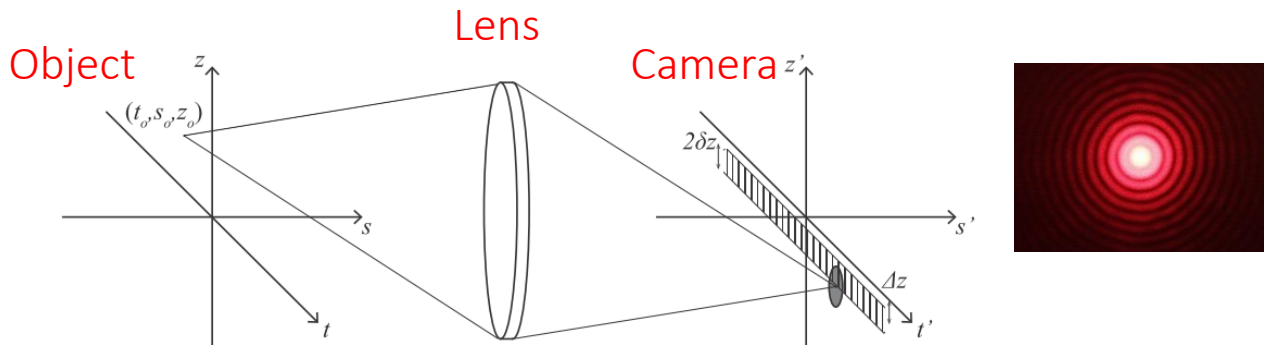
Diffraction

The (optical) depth of focus problem



Objects in focus are sharp, objects out of focus are blurred

Image resolution in optical tomography (I)

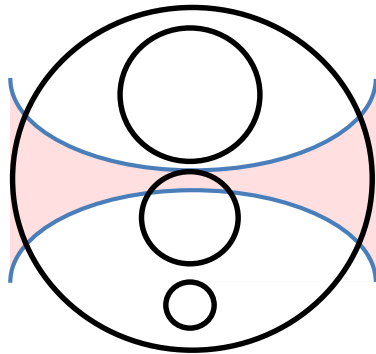


$$p(t', z') = \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} f(t' - t, s' - s, z' - z) |h(t, s, z)|^2 dt ds dz \Big|_{s'=0}$$

Convolution is integration over the object emission

Approximation:

Slide thickness > PSF width



Gaussian beam PSF

Image resolution in optical tomography (II)

Projection slice theorem:

$$FT_{1D}\{proj\{f\}\} = slice\{FT_{2D}\{f\}\}$$

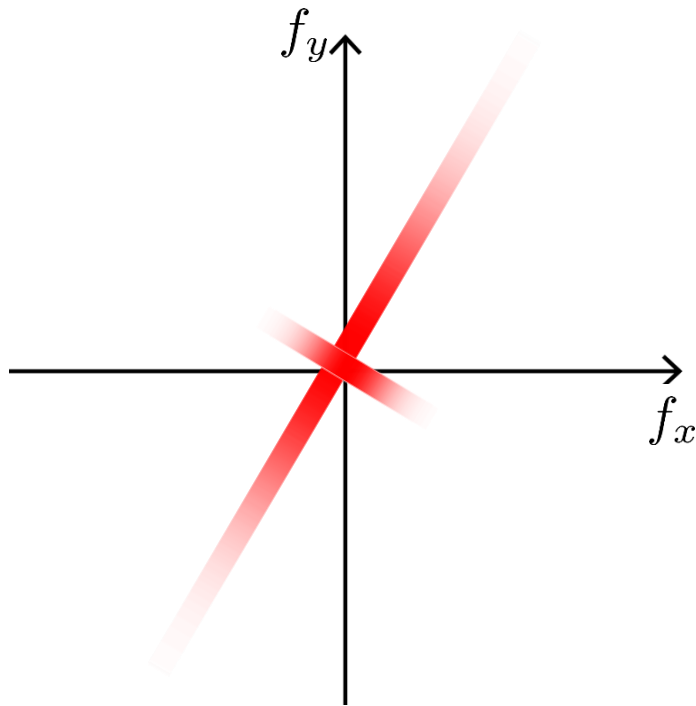
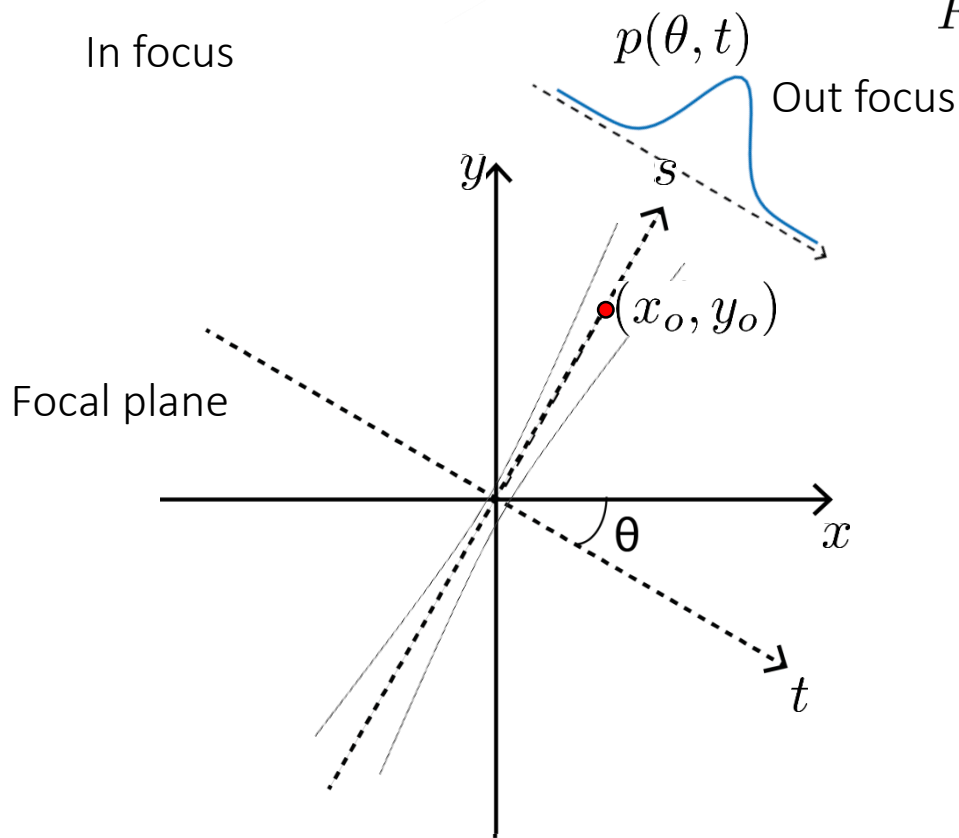


Image resolution in optical tomography (III)

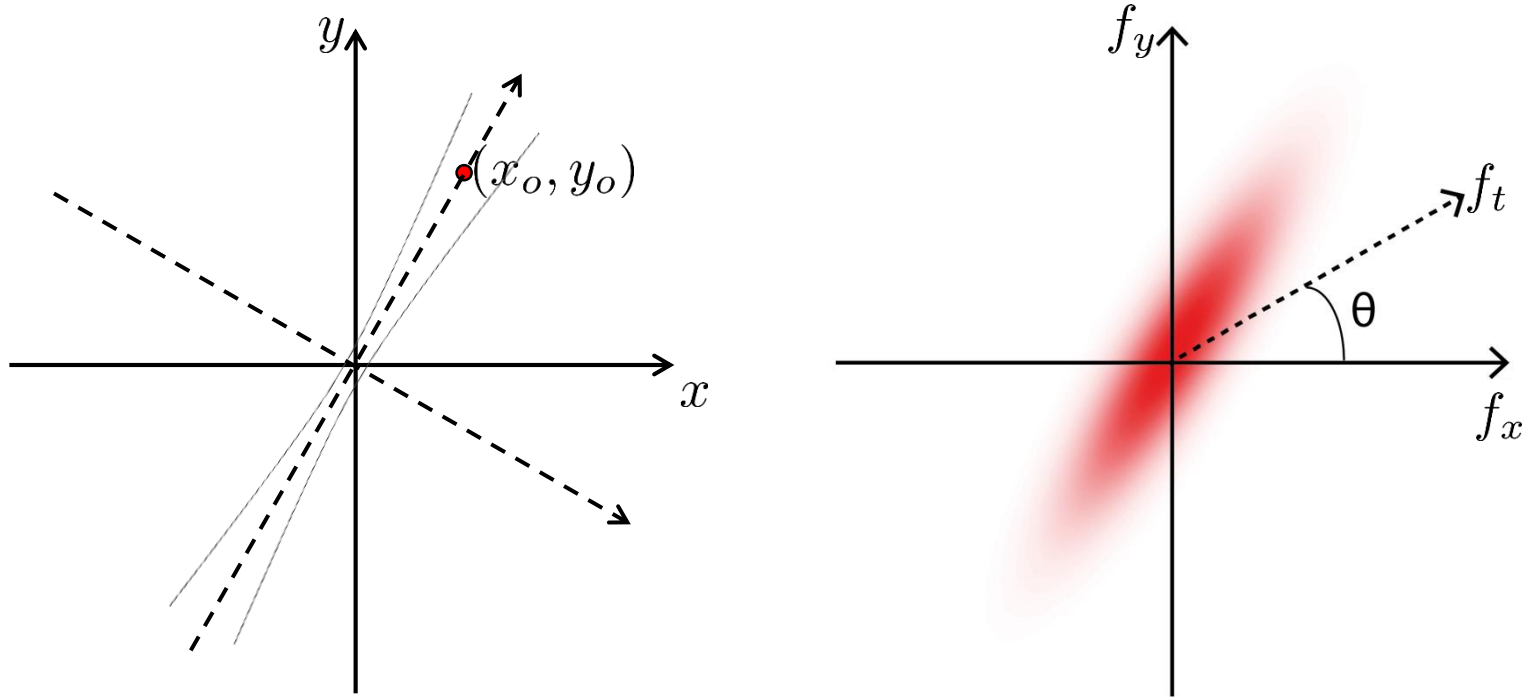


Image resolution in optical tomography (IV)

$$I_t(f_x, f_y) = \exp\left(-\frac{1}{2}\pi^2(f_x^2 + f_y^2) \left[w_0^2 + \frac{\lambda^2 r_i^2 \sin^2(\theta_i - \theta)}{\pi^2 w_0^2}\right]\right) \exp(-2\pi i(x_i f_x + y_i f_y))$$

Fourier transform of $I_t(f_x, f_y)$ is point spread function

$$PSF(u, v) = \sqrt{\frac{4}{\pi^2 w_0^2 \left(w_0^2 + \frac{\lambda^2 r_i^2}{\pi^2 w_0^2}\right)}} \exp\left(-\left[\frac{2u^2}{w_0^2} + \frac{2v^2}{\left(w_0^2 + \frac{\lambda^2 r_i^2}{\pi^2 w_0^2}\right)}\right]\right)$$

- reduction of impulse response in radial direction
- PSF width is independent of radial direction
- tangential PSF widens with increasing radial direction

Image resolution in optical tomography (V)

$w_0 = 10 \mu\text{m}$
 $\lambda = 545 \text{ nm}$
 $\text{NA} = 0.04$

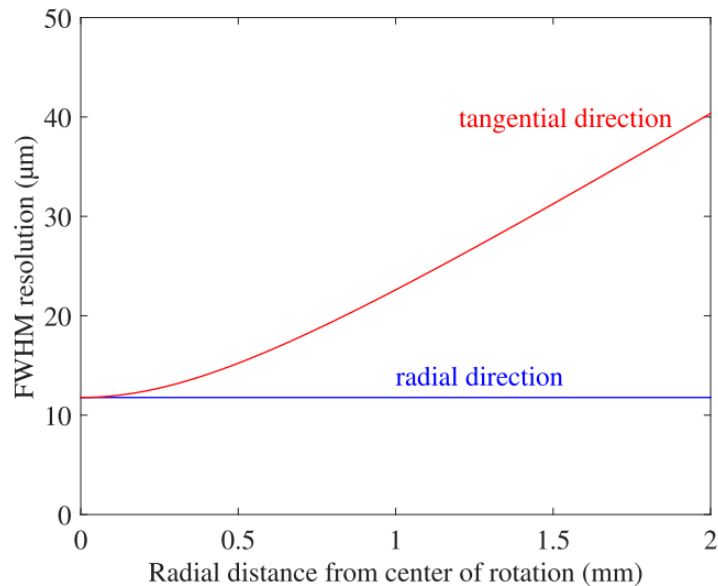
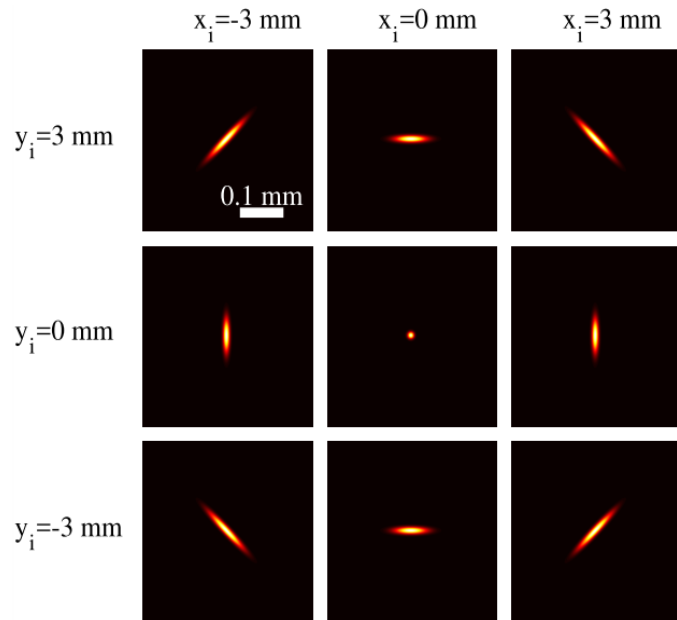
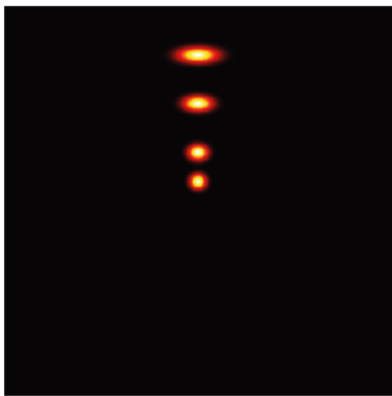


Image resolution in optical tomography (VI)

Input image = FBP reconstruction



Output image



Image resolution characterization

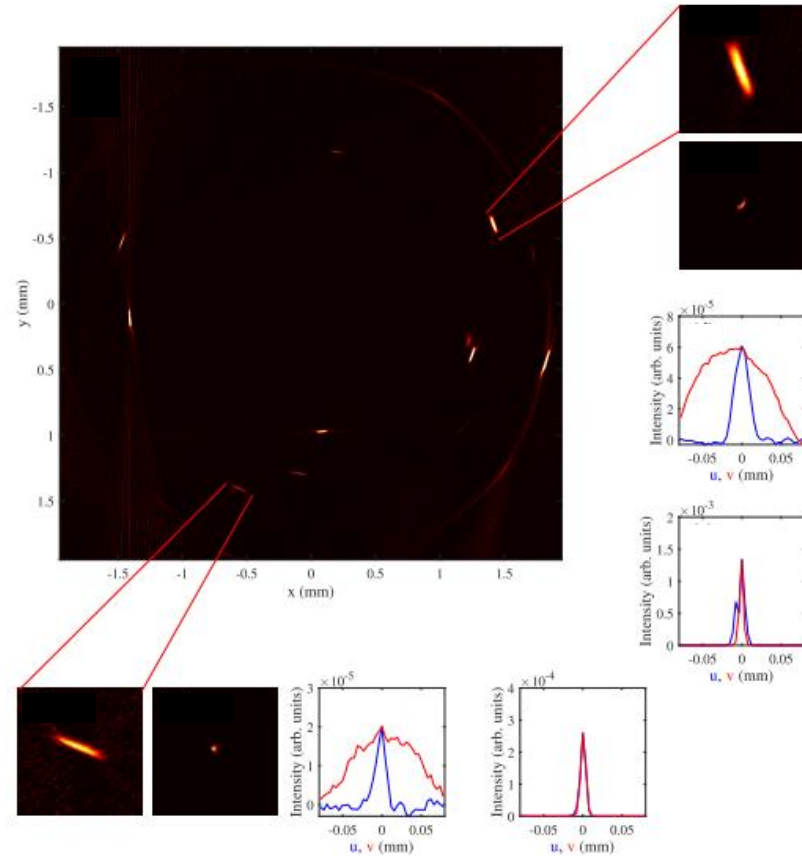
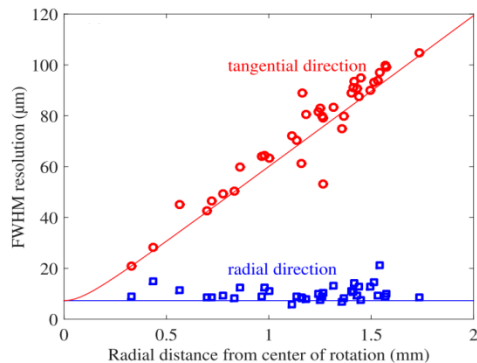
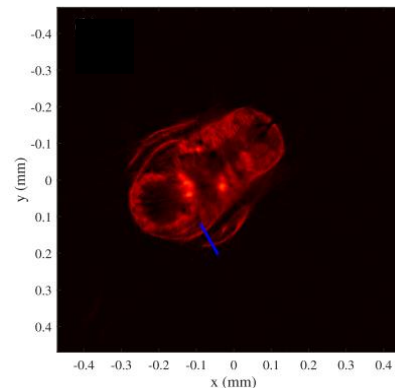


Image resolution and deconvolution

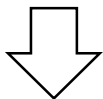
Fluorescent beads



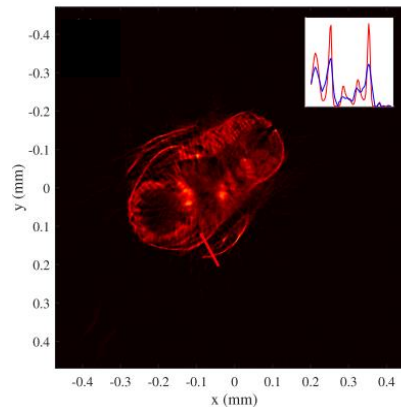
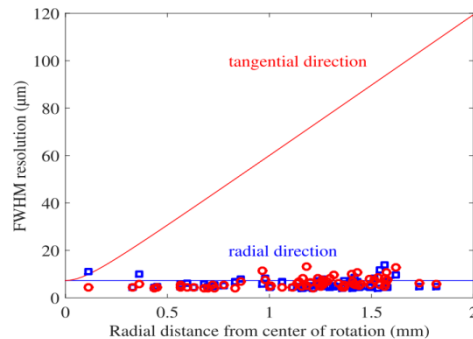
Zebrafish



Filtered
backprojection



FBP
+
convolution



Iterative tomographic reconstruction

Problem definition

$$p(s, \theta) = \int f[(x - s) \cos(\theta) + z \sin(\theta), (x - s) \cos(\theta) - z \sin(\theta)] |h(x, z)|^2 dx dz$$

Point spread function

Object (shifted and rotated)

Discretization

$$\mathbf{p} = \mathbf{A} \cdot \mathbf{f}$$

$$\mathbf{p} \in \mathbb{R}^{m \cdot n \times 1}$$

Vector of stacked projections

$$\mathbf{f} \in \mathbb{R}^{n \cdot n \times 1}$$

Vector of the object

$$\mathbf{A} \in \mathbb{R}^{m \cdot n \times n \cdot n}$$

Geometry matrix (size of the object x the number of angles)

Optimization

$$\min_{\mathbf{f}} \frac{1}{2} \|\mathbf{A} \cdot \mathbf{f} - \mathbf{p}\|_2^2$$

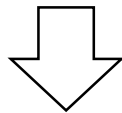
Measurement geometry

Object

Projection data

Iterative tomographic reconstruction

1000x1000 grid points in the object plane, 360 projections (1 per degree)



Projection data \mathbf{p} has size $(360 \times 1000) \times 1$

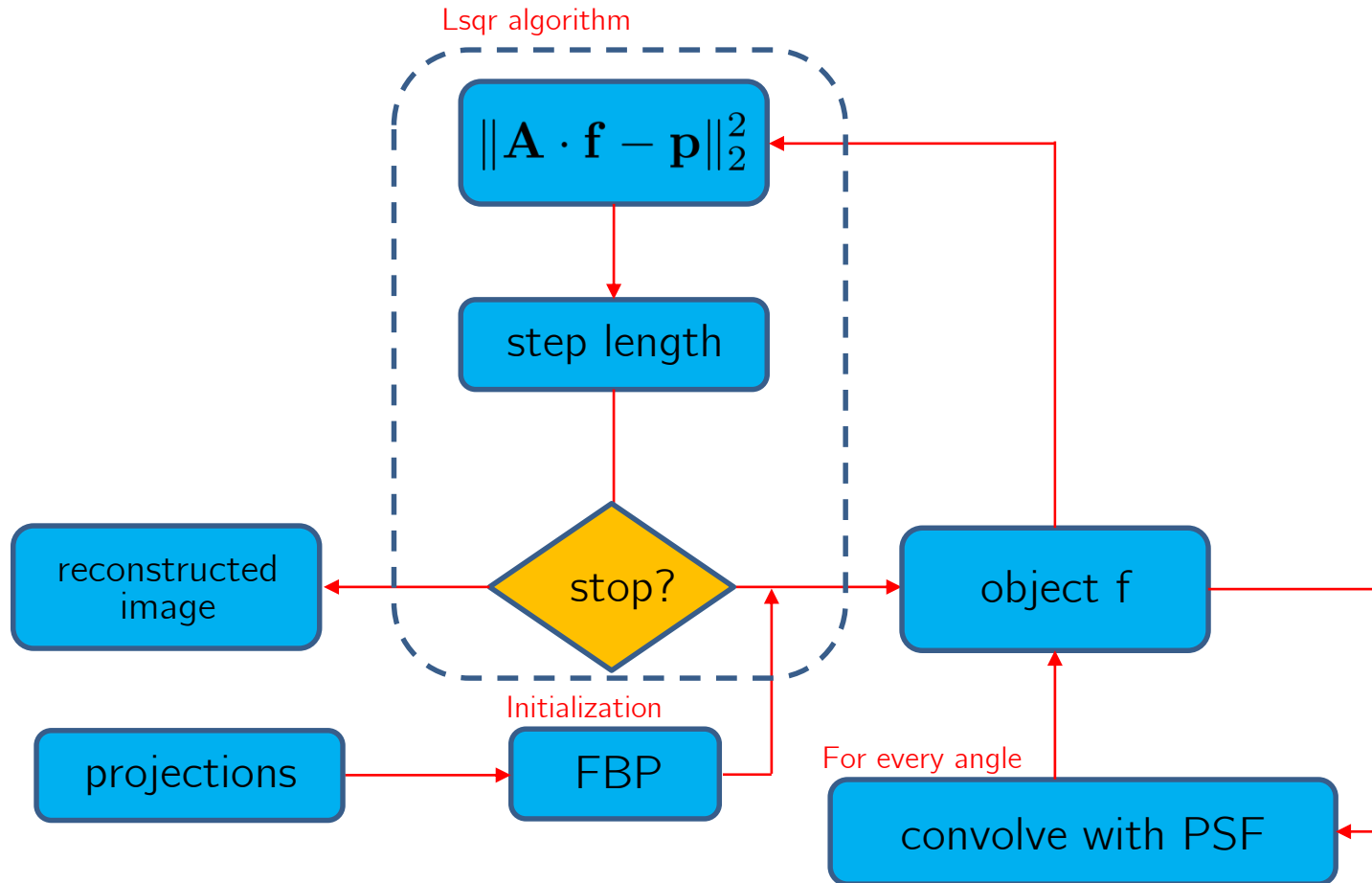
Object \mathbf{f} has size $(1000 \times 1000) \times 1$

Measurement geometry \mathbf{A} has size $(360 \times 1000) \times (1000 \times 1000) \approx 8$ terabyte

Solution

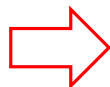
Calculate for every angle and lateral offset the difference $\|\mathbf{A} \cdot \mathbf{f} - \mathbf{p}\|_2^2$ and calculate the total merit value sequentially

Iterative reconstruction algorithm

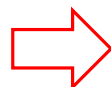


Optical tomographic reconstruction

Original Image

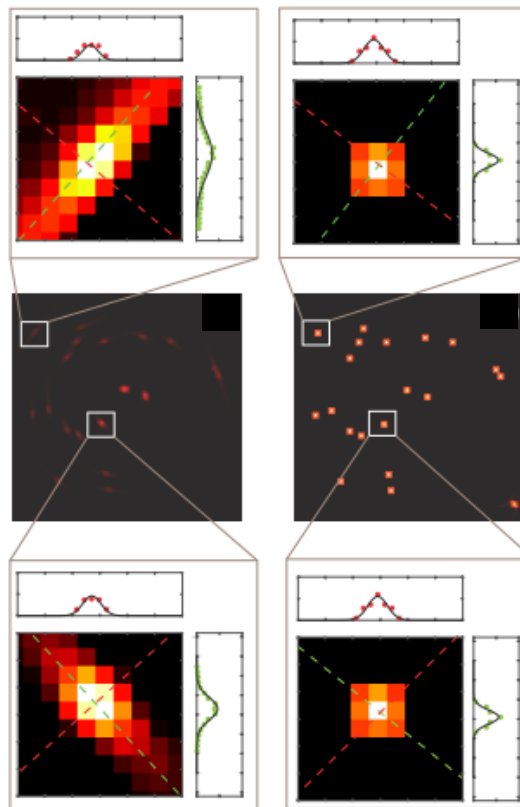


Calculate
blurred
projections



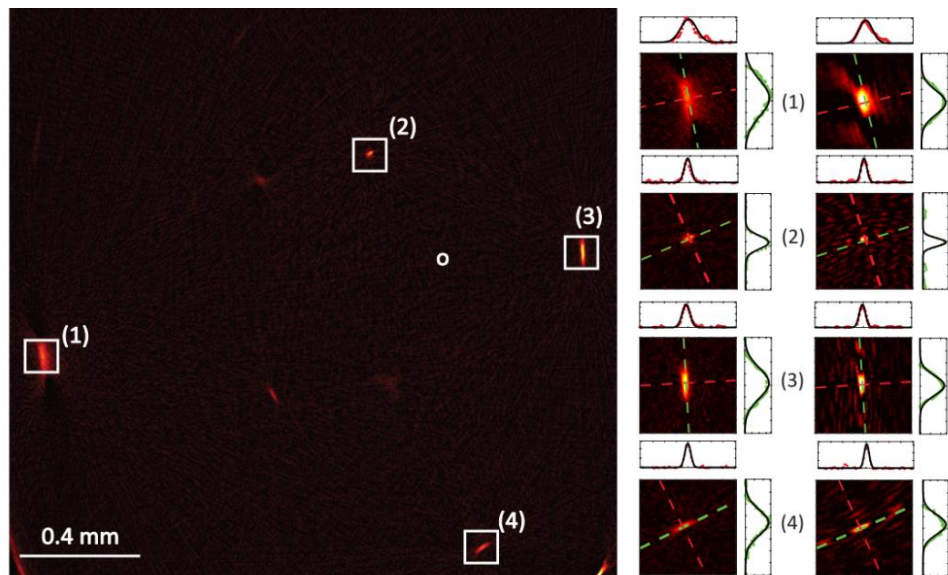
Filtered
back projection

PSF-based
reconstruction

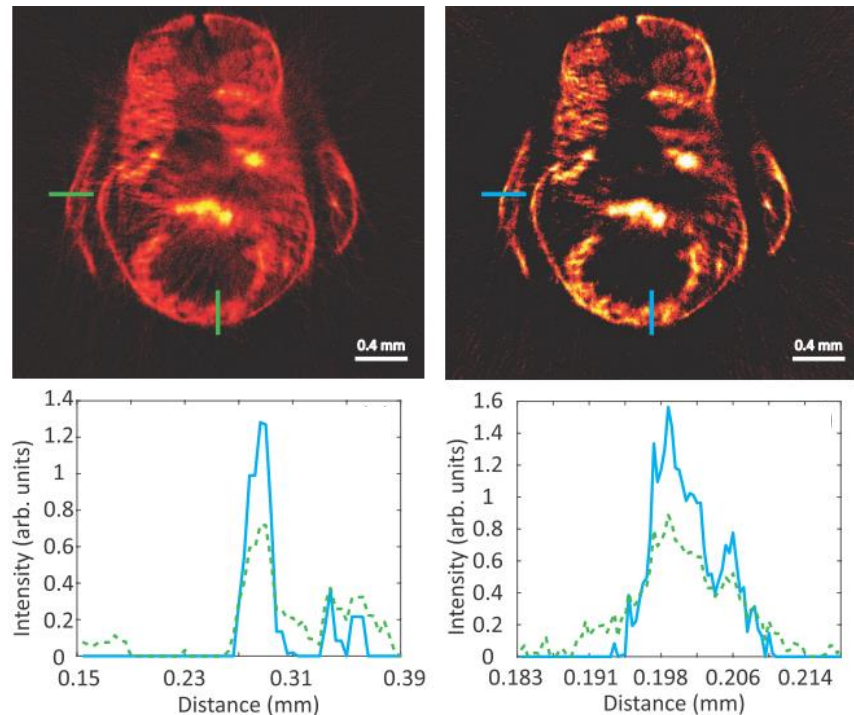


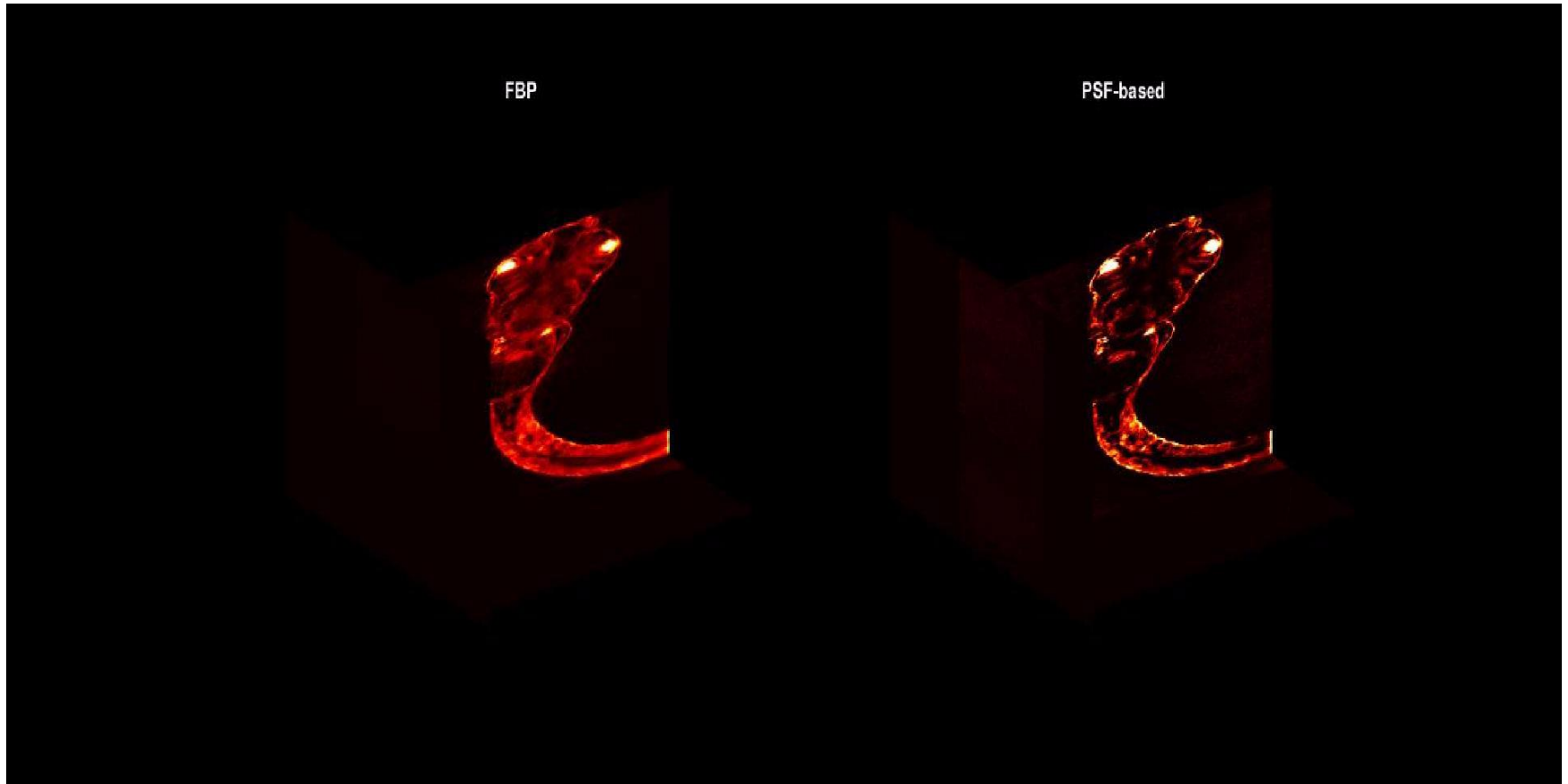
Optical tomographic reconstruction

Fluorescent beads



Zebrafish

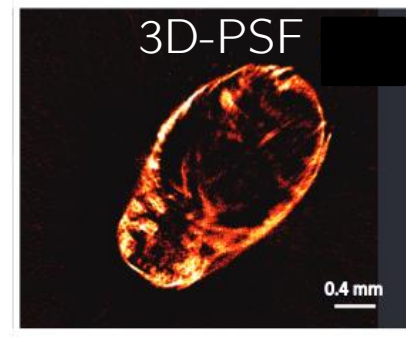
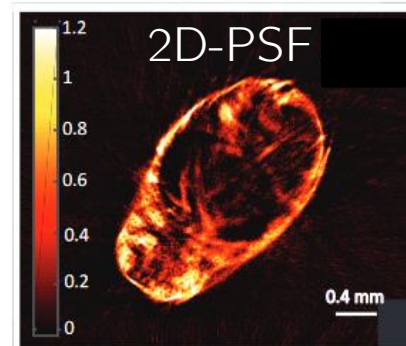
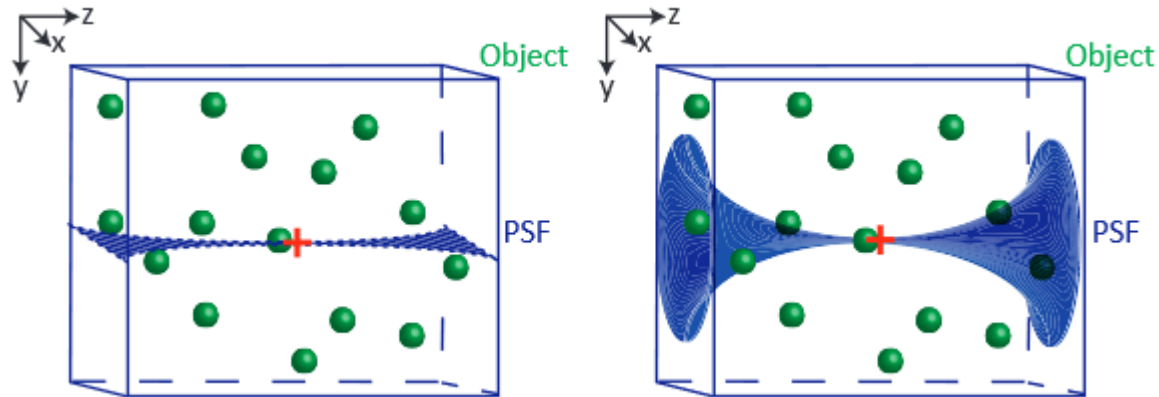




Point spread function based image reconstruction in optical projection tomography

A. K. Trull, J. van der Horst, W. J. Palenstijn, L. J. van Vliet, T. van Leeuwen, and J. Kalkman, *Physics in Medicine and Biology* 62, 7784 (2017)

The 3D problem reconstruction problem



Projection data

\mathbf{p} has size $(360 \times 950 \times 300) \times 1$

Object

\mathbf{f} has size $(950 \times 950 \times 300) \times 1$

Measurement geometry

\mathbf{A} has size $(360 \times 950 \times 300) \times (950 \times 950 \times 300)$

Summary and outlook

- Effects of diffraction in optical tomography can be compensated for
- Deconvolution approach is fast and gives best results for point objects
- PSF-based reconstruction is slower, but gives best results for extended objects

Future work

- Full 3D reconstruction
 - ✓ Fast & iterative gigavoxel reconstruction (non-separable)
- Multi-modal reconstruction
 - ✓ fluorescence + phase
- Multi-physics reconstruction
 - ✓ including beam propagation in the sample (refraction, diffraction)
 - ✓ including polarization