Unrolling Inference:

The Recurrent Inference Machine

Max Welling

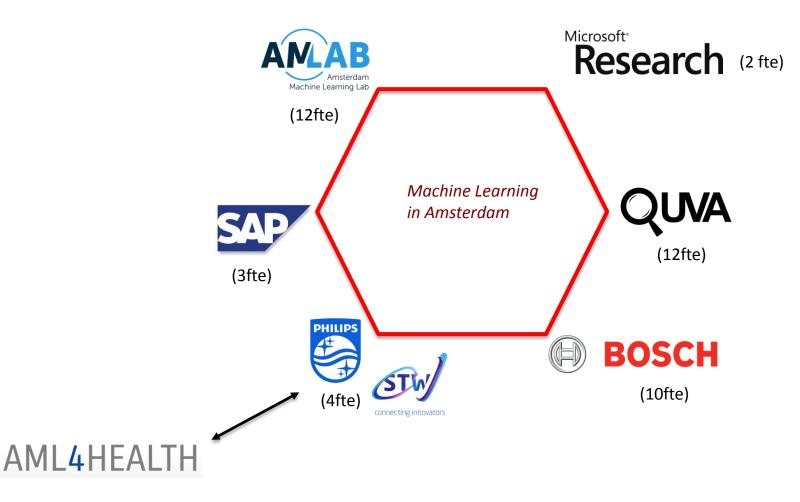
University of Amsterdam / Qualcomm



Canadian Institute for Advanced Research



ML @ UvA



Overview

- Meta learning
- Recurrent Inference Machine
- Application to MRI
- Application radio astronomy
- Conclusions

Learning to learn by gradient descent by gradient descent

2016

Marcin Andrychowicz¹, Misha Denil¹, Sergio Gómez Colmenarejo¹, Matthew W. Hoffman¹, David Pfau¹, Tom Schaul¹, Brendan Shillingford^{1,2}, Nando de Freitas^{1,2,3}

¹Google DeepMind ²University of Oxford ³Canadian Institute for Advanced Research

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• Train an optimizer to choose the best parameter updates by solving many optimization problems and learn the patterns.

 $\theta \leftarrow \theta + \eta_t \nabla_\theta F(\theta)$

• Unroll gradient optimizer, then abstract into a parameterized computation graph, e.g. RNN

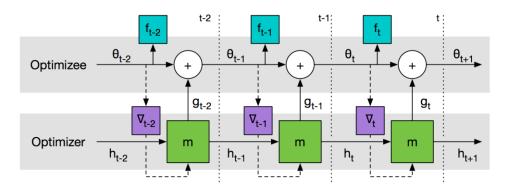


Figure 2: Computational graph used for computing the gradient of the optimizer.

Value Iteration Networks

2017

Aviv Tamar, Yi Wu, Garrett Thomas, Sergey Levine, and Pieter Abbeel

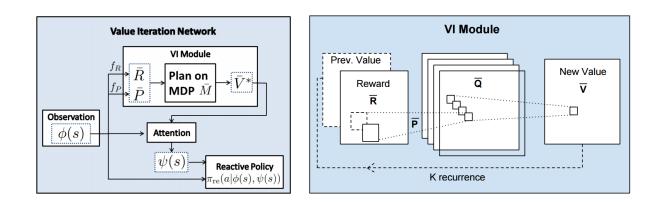
Dept. of Electrical Engineering and Computer Sciences, UC Berkeley

LEARNING TO REINFORCEMENT LEARN

JX Wang¹, Z Kurth-Nelson¹, D Tirumala¹, H Soyer¹, JZ Leibo¹, R Munos¹, C Blundell¹, D Kumaran^{1,3}, M Botvinick^{1,2} ¹DeepMind, London, UK ²Gatsby Computational Neuroscience Unit, UCL, London, UK ³Institute of Cognitive Neuroscience, UCL, London, UK

{wangjane, zebk, dhruvat, soyer, jzl, munos, cblundell, dkumaran, botvinick} @google.com

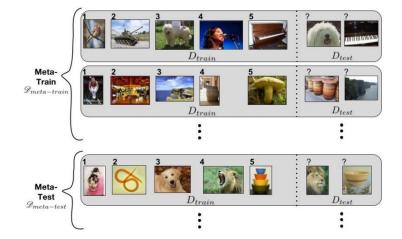
• Learning a planning algorithm to execute the best actions by solve many different RL.

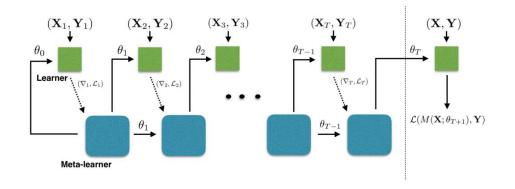


Optimization as a Model for Few-Shot Learning

Sachin Ravi* and Hugo Larochelle Twitter, Cambridge, USA {sachinr, hugo}@twitter.com

• One shot learning: meta-learn a learning algorithm to classify from very few examples



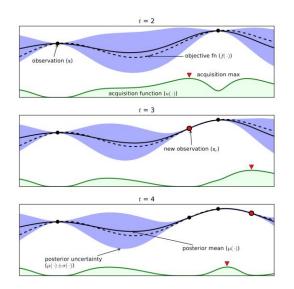


2017

NEURAL ARCHITECTURE SEARCH WITH 2017 REINFORCEMENT LEARNING

Barret Zoph^{*}, Quoc V. Le Google Brain {barretzoph,qvl}@google.com

• Learning a NN architecture using active learning / reinforcement learning



Number Filter Filter Stride Stride Number Filter of Filters Height Width Height Width of Filters Height Layer N-1 Layer N Layer N+1

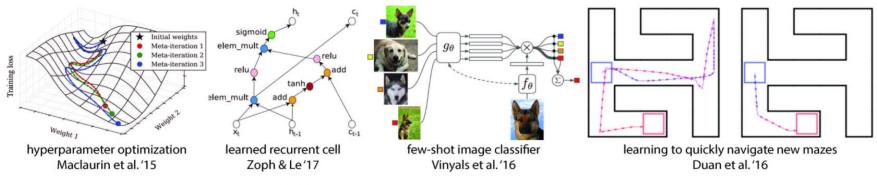
Bayesian optimization



BERKELEY ARTIFICIAL INTELLIGENCE RESEARCH

Learning to Learn

Chelsea Finn Jul 18, 2017



Various recent meta-learning approaches.

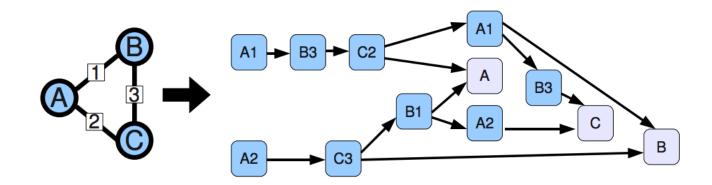
The Recipe



- Study the classical iterative optimization algorithm
- Unroll the computation tree and cut it off at T steps (layers)
- Generalize / parameterize the individual steps
- Create targets at the last layer
- Backpropagate through the "deep network" to fit the parameters
- Execute the network to make predictions

Learning to Infer

- Unroll a known iterative inference scheme (e.g. mean field, belief propagation)
- Abstract into parameterized computation graph for fixed nr. iterations, e.g. RNN
- Learn parameters of RNN using meta-learning (e.g. solving many inference problems)



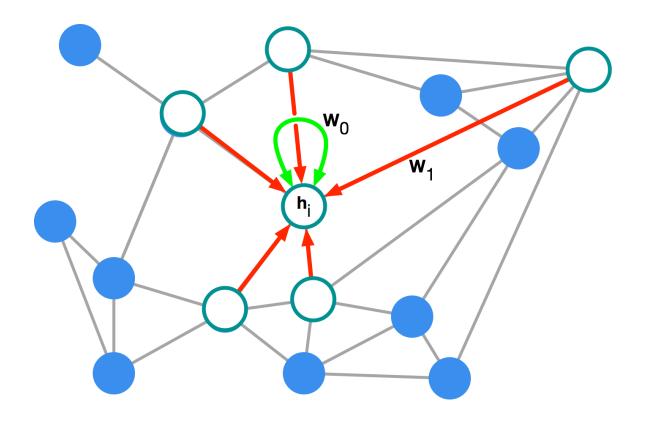
Learning Message-Passing Inference Machines for Structured Prediction

Stéphane Ross Daniel Munoz Martial Hebert J. Andrew Bagnell The Robotics Institute, Carnegie Mellon University stephaneross@cmu.edu, {dmunoz, hebert, dbagnell}@ri.cmu.edu

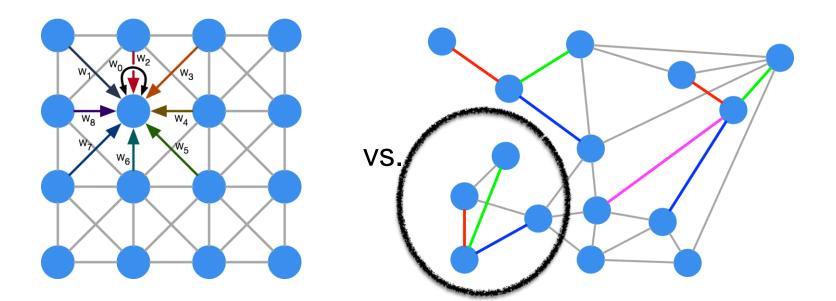
Graph Convolutions



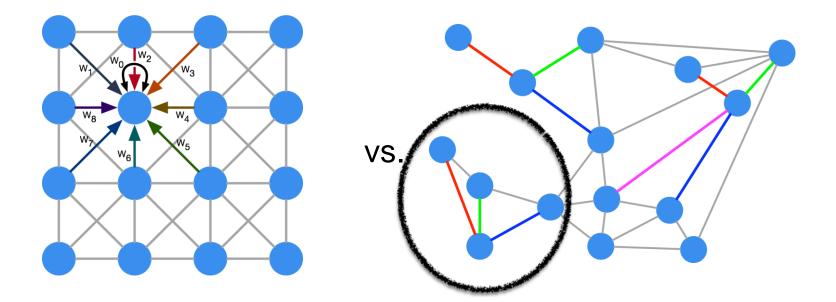
Thomas Kipf



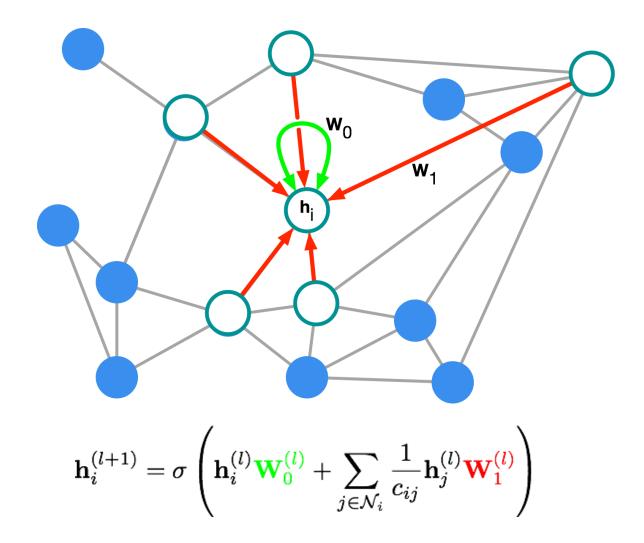
Convolutions vs Graph Convolutions



Convolutions vs Graph Convolutions

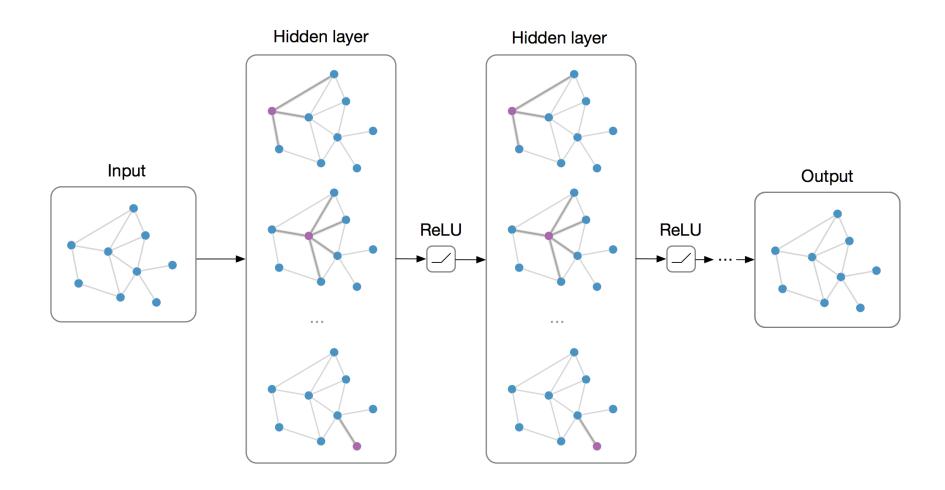


Graph Convolutions



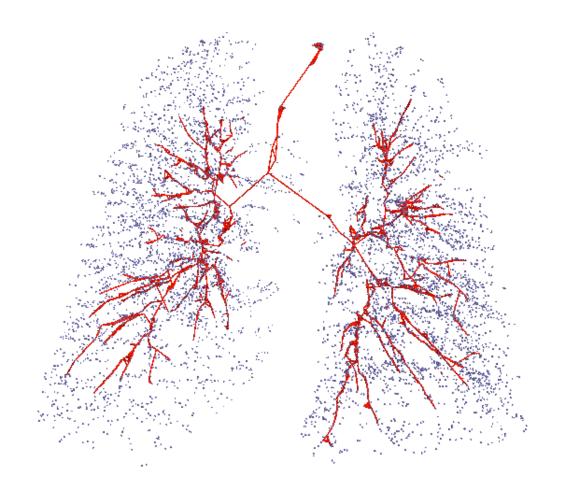
Graph Convolutional Networks

Kipf & Welling ICLR (2017)



Application to Airway Segmentation

(work in progress, with Rajhav Selvan & Thomas Kipf)



Inverse Problems



w/ Patrick Putzky

Quantity of interest Measurement Forward Model

Forward Model $\mathbf{y} = g(\mathbf{x}) + n$

Inverse Model $\hat{\mathbf{x}} = h(\mathbf{y})$

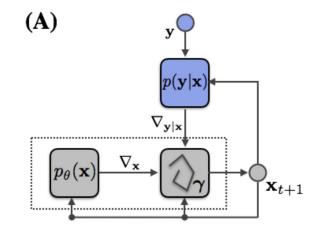
The Usual Approach

$$\begin{split} L(X) &= \log P_A(Y|X) + \log P_\theta(X) \\ Y &= A \cdot X + \eta \\ \uparrow & \uparrow \\ \text{observations} \\ \end{split} \quad \text{generative model (known)} \end{split}$$

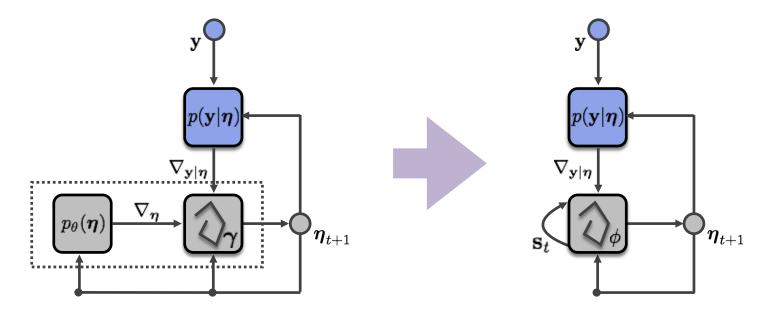
$$X_{t+1} = X_t + \alpha_t (\nabla_X \log P_A(Y|X_t) + \nabla_X \log P_\theta(X_t))$$

advantage: model P(X) and optimization are separated.

disadvantage: accuracy suffers because model and optimization interact...



Learning Inference: Recurrent Inference Machine

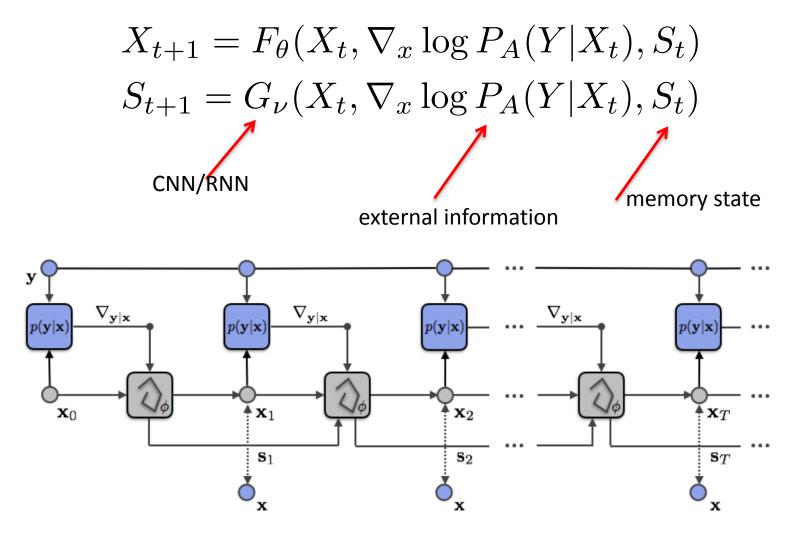


 $\boldsymbol{\eta}_{t+1} = \boldsymbol{\eta}_t + \gamma_t (\nabla_{\mathbf{y}|\boldsymbol{\eta}} + \nabla_{\boldsymbol{\eta}}) \qquad \qquad \boldsymbol{\eta}_{t+1} = \boldsymbol{\eta}_t + h_\phi (\nabla_{\mathbf{y}|\boldsymbol{\eta}}, \boldsymbol{\eta}_t, \mathbf{s}_t)$

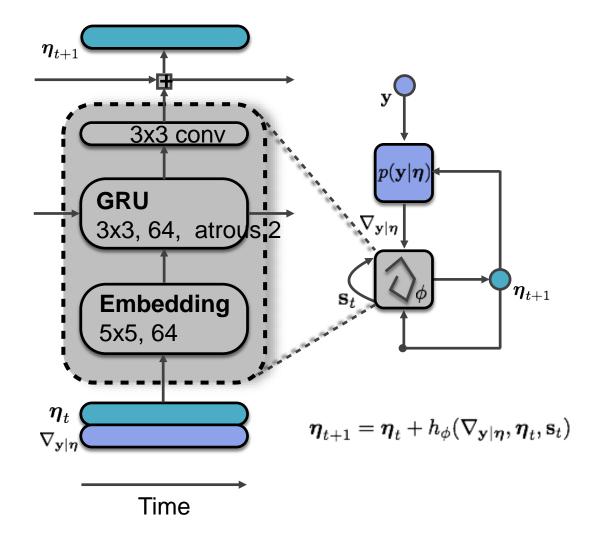
- Abstract and parameterize computation graph into RNN
- Integrate prior P(X) in RNN
- Add memory state s
- Meta learn the parameters of the RNN

Recurrent Inference Machine (RIM)

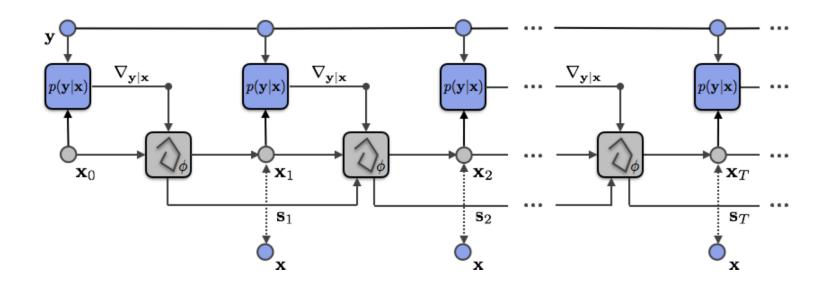
Learn to optimize using a RNN.



Recurrent Inference Machine

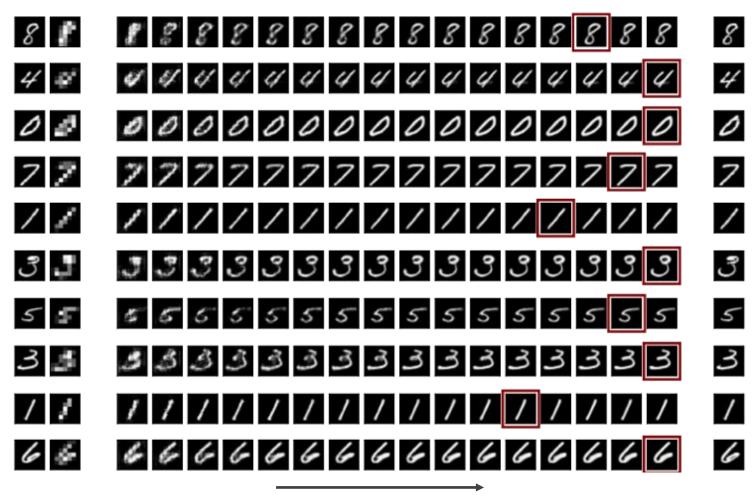


Recurrent Inference Machines in Time



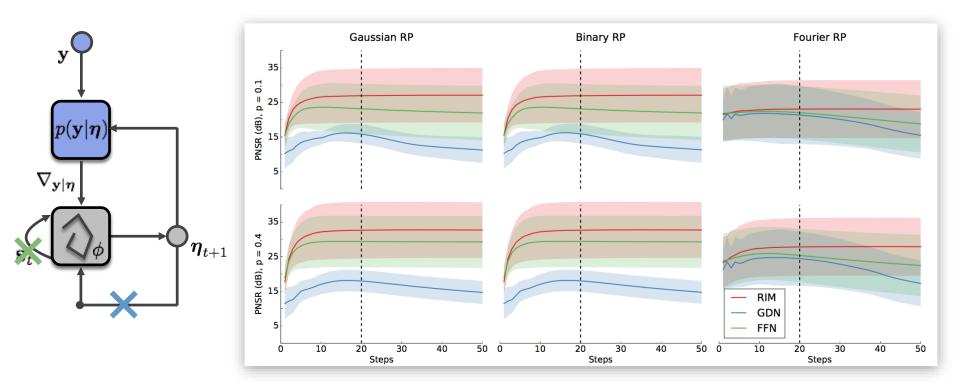
Objective $g(\phi) = \frac{1}{2} \sum_{i=1}^{N} \sum_{t=1}^{T} (\mathbf{x}^{(i)} - \hat{\mathbf{x}}_{t}^{(i)})$

Simple Super-Resolution



Time

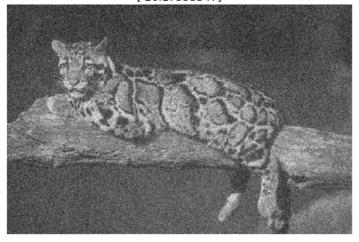
Reconstruction from Random Projections



32 x 32 pixel image patches Fast Convergence on all tasks

Image Denoising





EPLL: [29.11631168]

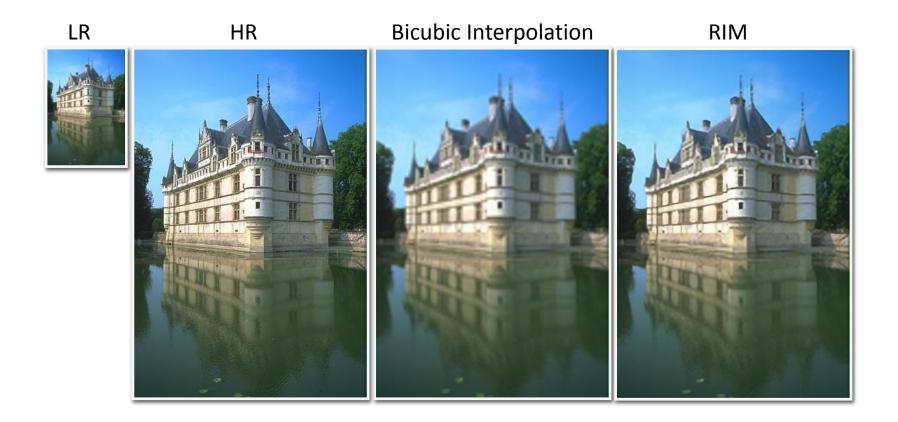




Denoising trained on small image patches, generalises to full-sized images

[20.17553347]

Super-resolution



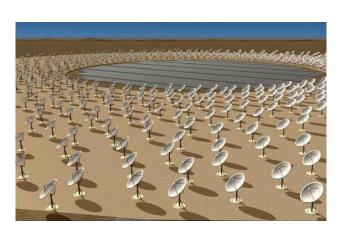
Super-resolution

		(a) Original Image	(b) Bicubic	(b) Bicubic: 30.43/0.8326		0.8660
						2
		(d) A+: 31.43/0.8676	(e) SelfExSt	R: 31.18/0.8656	(f) RIM: 31.59/0	.8712
Metric	Scale	Bicubic	SRCNN	A+	SelfExSR	RIM (Ours)
PSNR	2x	29.55 ± 0.35	31.11 ± 0.39	31.22 ± 0.40	31.18 ± 0.39	31.39 ± 0.39
	3x	27.20 ± 0.33	28.20 ± 0.36	28.30 ± 0.37	28.30 ± 0.37	28.51 ± 0.37
	4x	25.96 ± 0.33	26.70 ± 0.34	26.82 ± 0.35	26.85 ± 0.36	27.01 ± 0.35
SSIM	2x	0.8425 ± 0.0078	0.8835 ± 0.0062	0.8862 ± 0.0063	0.8855 ± 0.0064	0.8885 ± 0.0062
	3x	0.7382 ± 0.0114	0.7794 ± 0.0102	0.7836 ± 0.0104	0.7843 ± 0.0104	0.7888 ± 0.0101
	4x	0.6672 ± 0.0131	0.7018 ± 0.0125	0.7089 ± 0.0125	0.7108 ± 0.0124	0.7156 ± 0.0125

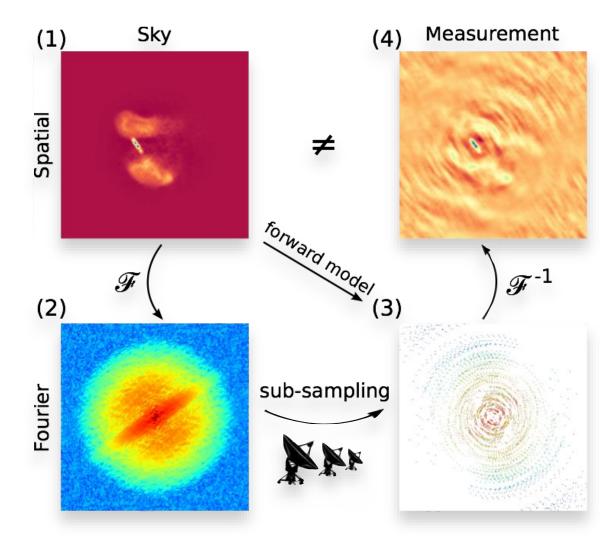


Square Kilometer Array

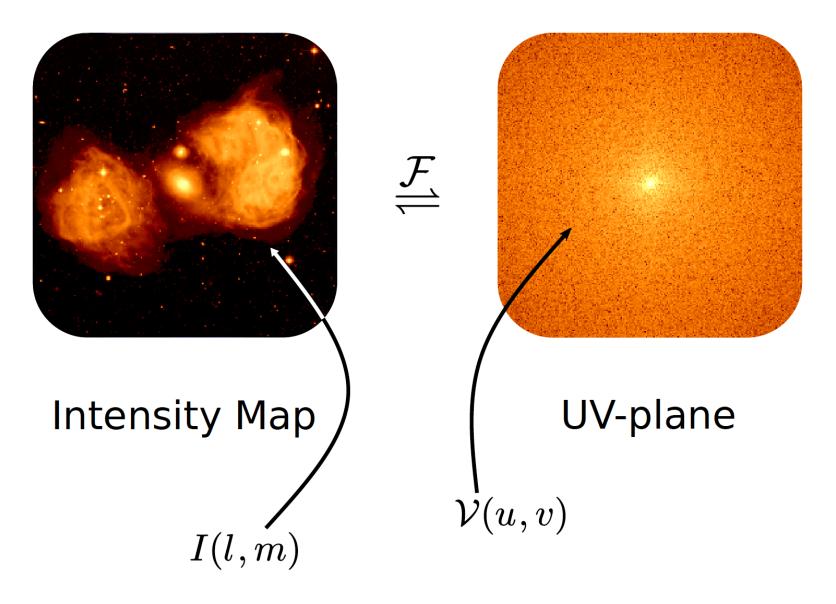
Jorn Peters



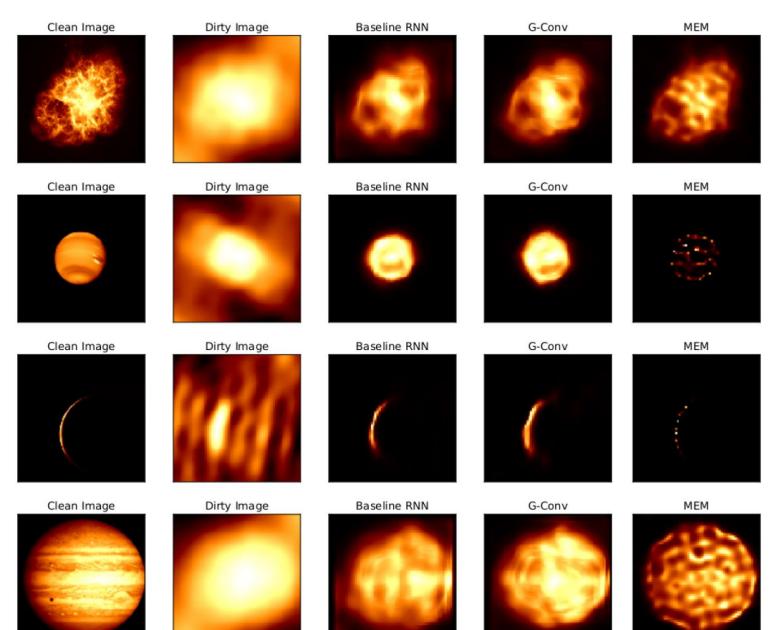
Up to 14.4 Gigapixels With thousands of Channels



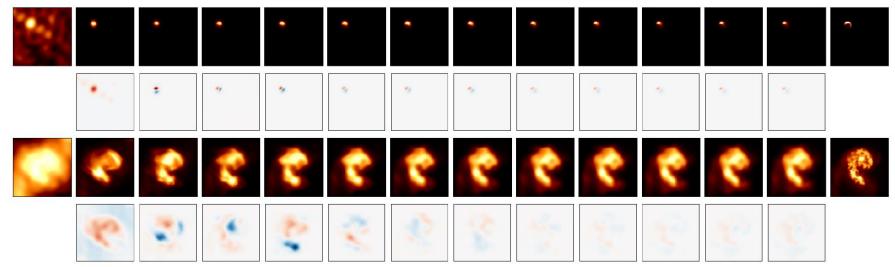
Radio Astronomy: Observations



Experiments: VLBI Inverse Models

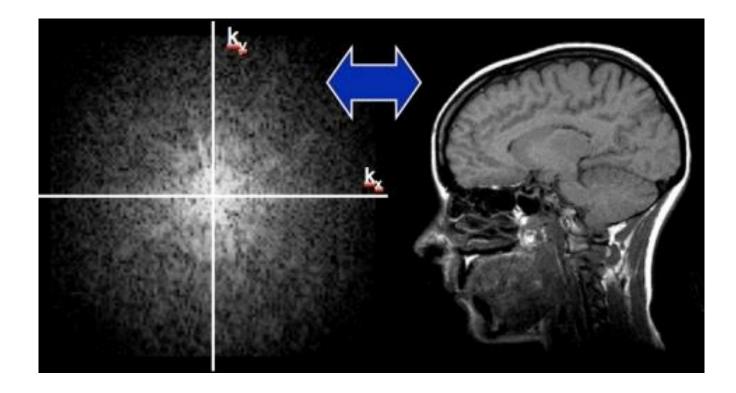


Direct Fourier Transform Forward Model



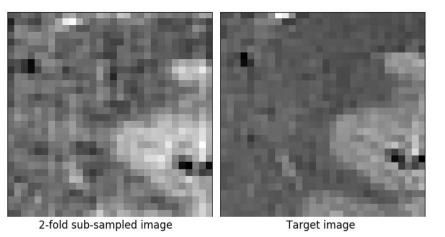
Deep Learning for Inverse Problems

w/ Kai Lonning & Matthan Caan



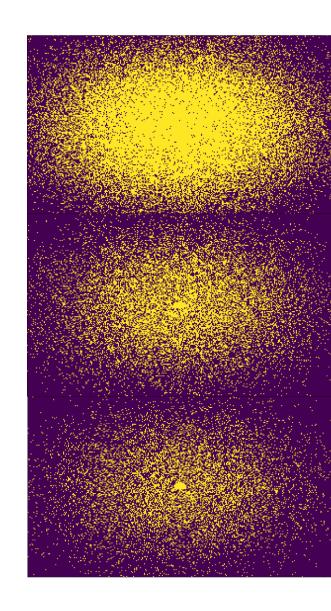
E.g. MRI Image Reconstruction

http://sbt.science.uva.nl/mri/about/



Example of training data point, 30x30 image patch

Testing done on full images, subsampling masks shown for 6x, 4x and 2x acceleration

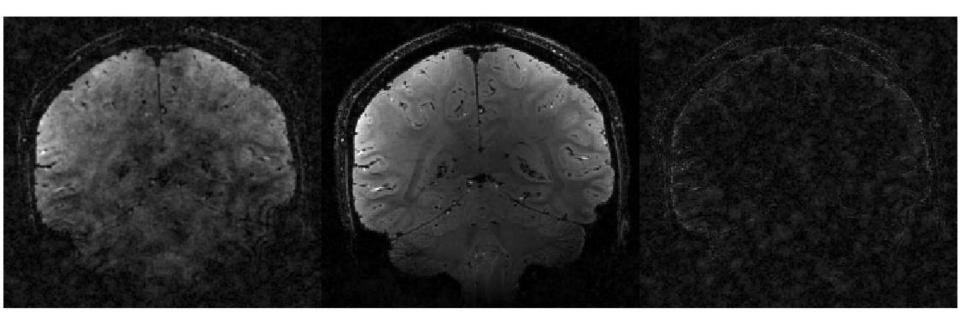


4x RVNN relu 8T 256F 0.005 4x CVNN cardioid 8T 128F 6x RVNN relu 8T 256F 6x CVNN cardioid 8T 128F 0.004 0.003 OS And the second se 0.002 0.001 2500 10000 17500 0 5000 7500 12500 15000 20000 train-step

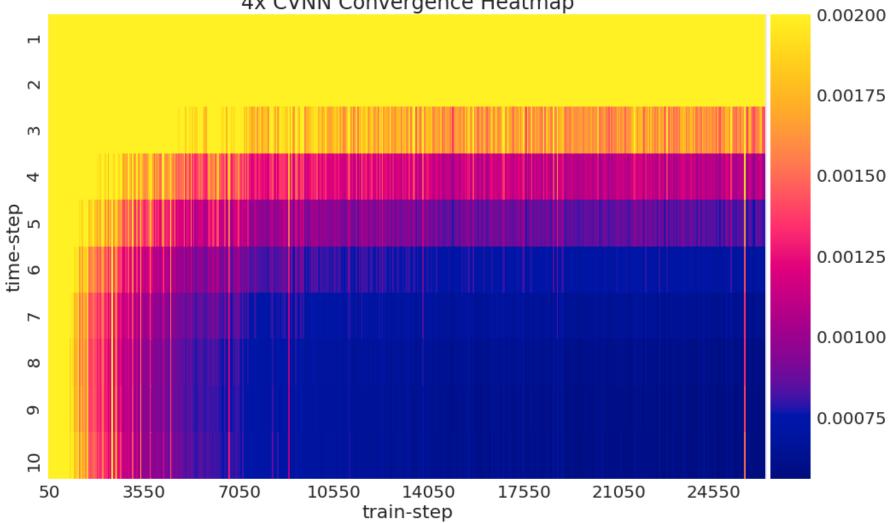
RIM test curves



A full brain RIM reconstruction, starting from the 4 times sub-sampled corruption on the left, attempting to recover the target on the right.

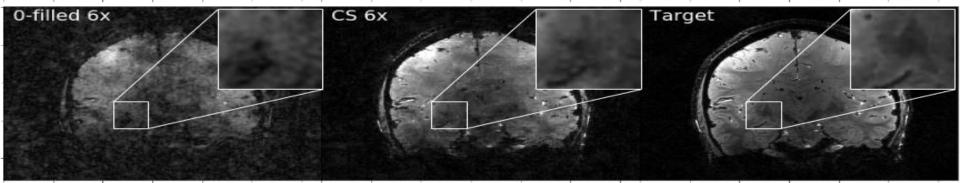


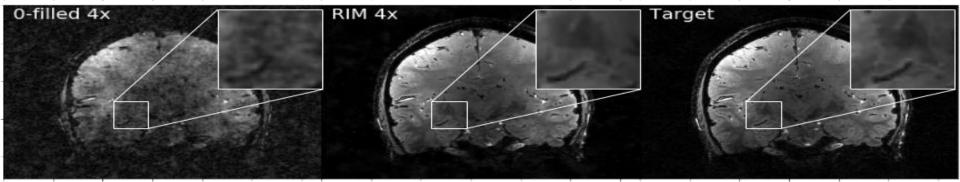
Each time-step in the Recurrent Inference Machine produces a new estimate, here shown to the left, from the 3x accelerated corruption until the 10th and final reconstruction. Target is in the middle, while the error (not to scale) is shown to the right.

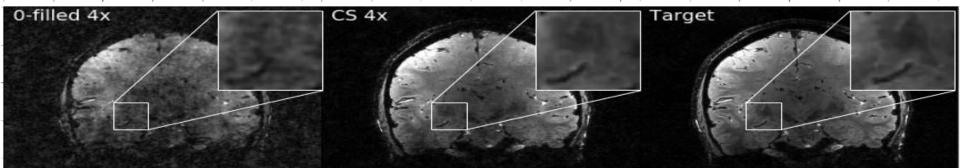


4x CVNN Convergence Heatmap

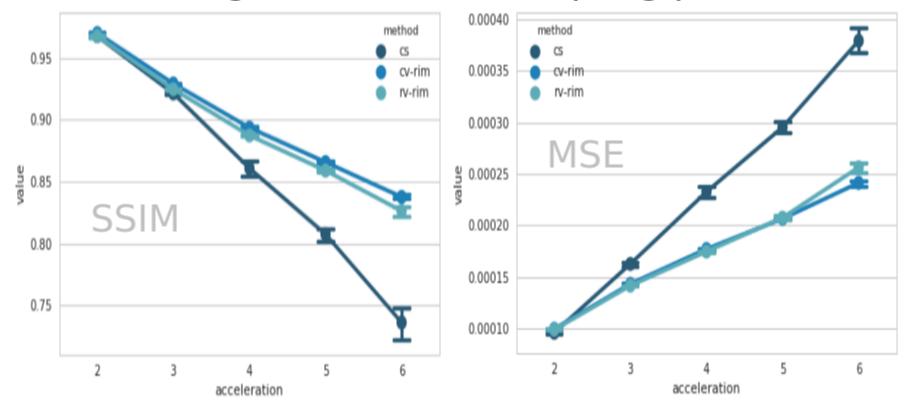




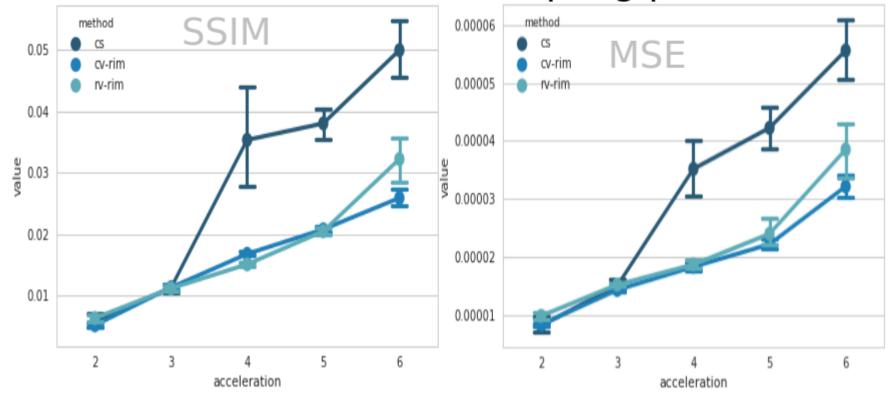




Average across sub-sampling patterns



Std across sub-sampling patterns



Conclusions

- Meta learning is interesting new paradigm that can improve classical optimization and inference algorithms by exploiting patterns in classes of problems.
- RIM is a method that unrolls inference and learns to solve inverse problems.
- Great potential to improve & speed up radio-astronomy and MRI image reconstruction.
- Application to MRI-linac?

MRI-Guided Radiation Therapy

The promise of real-time visualization during radiotherapy treatment is pushing science and industry to develop exciting new advances in this cutting-edge technology



Elekta's MR-linac combines two technologies — an MRI scanner and a linear accelerator — in a single system. This allows physicians to precisely locate tumors, tailor the shape of X-ray beams and accurately deliver doses of radiation evento moving tumors.